#### University of North Georgia Nineteenth Annual Sophomore Level Mathematics Tournament April 6, 2013

A square and a circle intersect so that each side of the square contains a chord of the circle which equals the circle's radius. What is the ratio of the area of the square to the area of the circle? (Leave answer in terms of  $\pi$ .)



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Suppose the coefficients of  $x^3$  and  $x^4$  of a polynomial

 $(x+a)^5$  are the same and suppose a > 0.

Find the value of *a*.

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Two squares are nestled as shown and form 4 congruent triangles. The large square's area is 400 square units. What is the small square's area?





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A regular pentagon is inscribed in a circle of area  $16\pi cm^2$ . Find the perimeter of the pentagon approximated to the nearest tenth of a *cm*.



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A cyclist travels downhill at a speed of 12 *mph*, on the level part of the road at

8 mph, and uphill at 6 mph. She takes 4 hours to travel from town M to town N.

The return trip takes 4.5 hours. Find the distance between the two towns.